

COURSE NAME		Basic algebraic structures			
Code	PMM715	Year of study	3rd year of undergraduate study and 2nd year of graduate study		
Course teacher	Gordan Radobolja	Credits (ECTS)	6,0		
Associate teachers		Type of instruction (number of hours)	L	S	E
			30		30
Status of the course	required, elective	Percentage of application of e-learning			
COURSE DESCRIPTION					
Course objectives					
Course enrolment requirements and entry competences required for the course	Prerequisites: completed courses Introduction to Algebra with Analytic Geometry or Linear algebra and Matrix Calculus  Required competencies: knowledge of fundamentals of linear algebra and elementary mathematics.				
Learning outcomes expected at the level of the course (4 to 10 learning outcomes)	It is expected that the student will be able to: <ul style="list-style-type: none"> <li>• Distinguish between a formal polynomial and a polynomial function</li> <li>• Check reducibility of and factorise a rational polynomial</li> <li>• Apply Euclidean algorithm</li> <li>• Solve cubics and quartics</li> <li>• Explain the concept of solvability in radicals</li> <li>• Find Galois group of simple polynomials</li> <li>• State basic definitions and theorems in theory of commutative rings</li> <li>• Distinguish algebraic and transcendental numbers</li> <li>• Distinguish from algebraically closed and open fields</li> </ul>				
Course content broken down in detail by weekly class schedule (syllabus)	<b>Classical algebra (4 hours)</b> <ol style="list-style-type: none"> <li>1. Elementary number theory. Pythagorean triples, fundamental theorem of arithmetic.</li> <li>2. Number systems. Complex numbers. Roots of unity.</li> </ol> <b>Commutative rings (6 hours)</b> <ol style="list-style-type: none"> <li>3. Basics</li> <li>4. Domains and rings of fractions</li> <li>5. Polynomial ring and polynomial functions</li> <li>6. Homomorphisms</li> </ol> <b>Arithmetic of polynomials (8 hours)</b> <ol style="list-style-type: none"> <li>7. Divisibility</li> <li>8. Roots</li> <li>9. Factorisation</li> <li>10. Irreducibility and criteria. Cyclotomic polynomials</li> </ol> <b>Field theory (8 hours)</b> <ol style="list-style-type: none"> <li>11. Quotient ring</li> <li>12. Field extensions</li> <li>13. Algebraic extensions</li> <li>14. Splitting fields</li> </ol> <b>Solvability in radicals (4 hours)</b> <ol style="list-style-type: none"> <li>15. Groups</li> <li>16. Radical extensions</li> <li>17. Galois theory</li> </ol>				

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Format of instruction	Lectures and tutorial sessions.
Student responsibilities	Class attendance and partial written exams.
Screening student work ( <i>name the proportion of ECTS credits for each activity so that the total number of ECTS credits is equal to the ECTS value of the course</i> )	Class attendance: 2 ECTS Partial written exams: 2 ECTS Final exam: 2 ECTS
Grading and evaluating student work in class and at the final exam	Partial written exams and final written and oral exam. Positive grade of the written exam is required to take the oral exam.
Required literature (available in the library and via other media)	A. Cuoco, J. J. Rotman, <i>Learning modern algebra</i>
Optional literature (at the time of submission of study programme proposal)	D.S. Dummit, R.M. Foote, <i>Abstract Algebra</i> , treće izdanje, John Wiley and Sons, 2004.
Quality assurance methods that ensure the acquisition of exit competences	Anonymous student evaluations at the end of semester according to the regulations of the University of Split.
Other (as the proposer wishes to add)	